

Graphical models in image understanding



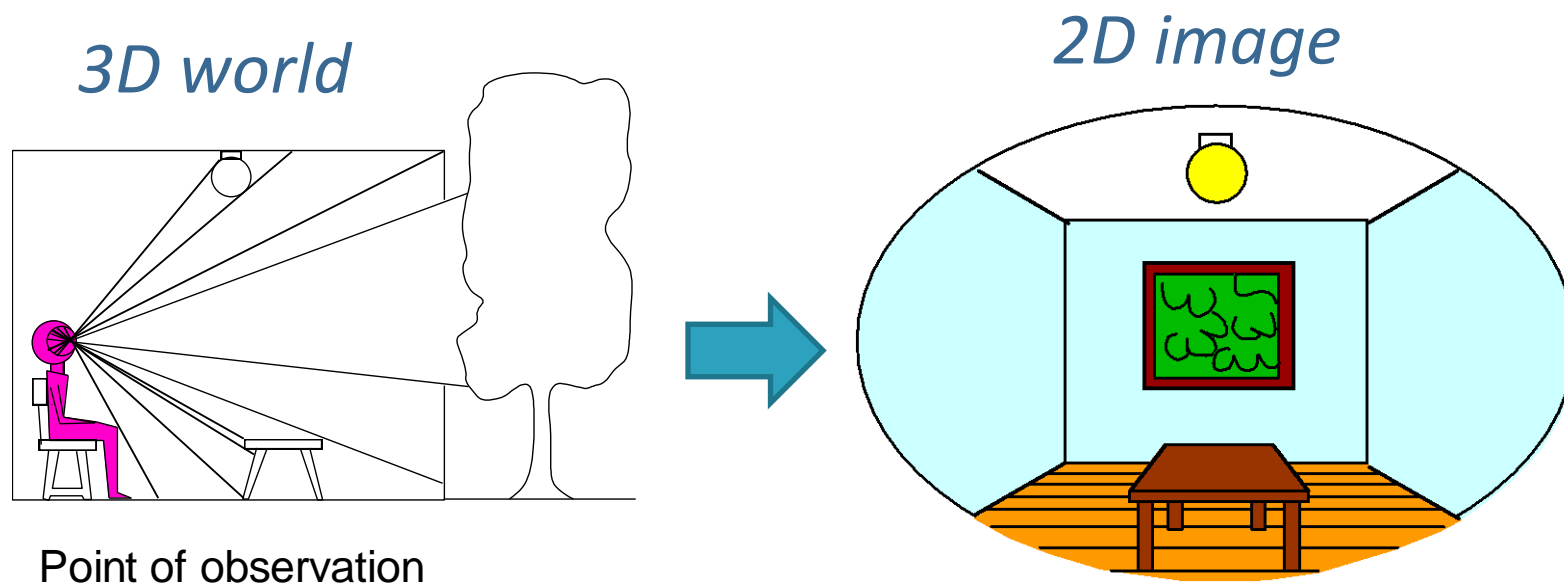
Olga Barinova

Lomonosov Moscow State University

Thanks to Anton Konushin for some slides

Why is image understanding difficult?

- Dimensionality reduction



What do we lose in perspective projection?

- Angles
- Distances and lengths

Why is image understanding difficult?

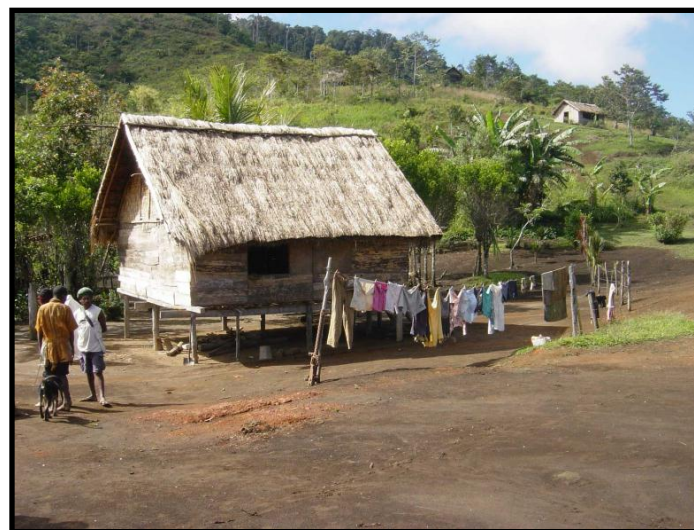
- Dimensionality reduction

The same 2D image can correspond to different 3D scenes



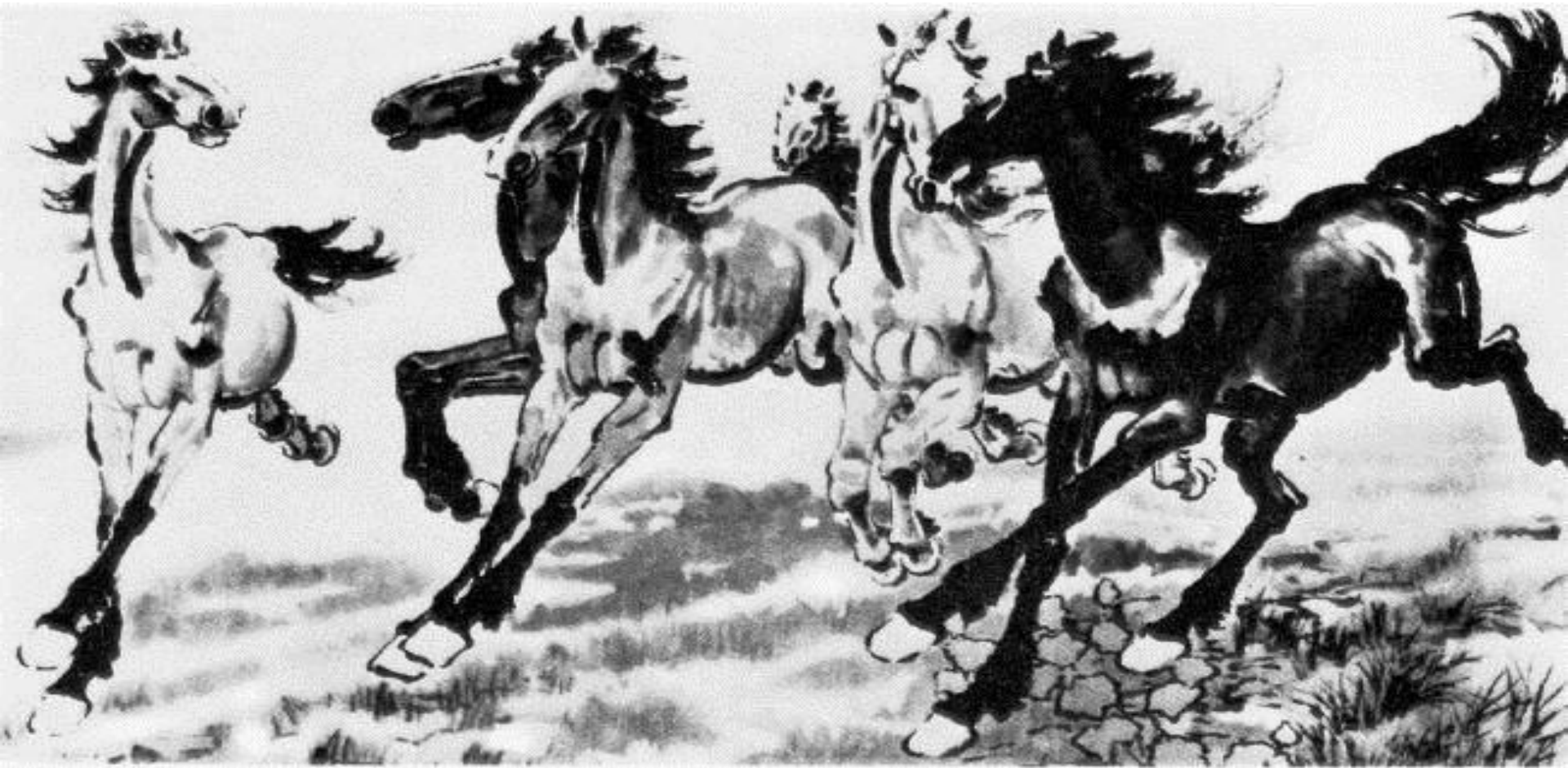
Why is image understanding difficult?

- Variability: interclass variability of appearance



Why is image understanding difficult?

- Variability: deformations and occlusions



Xu, Beihong 1943

Why is image understanding difficult?

- Variability: different viewpoints

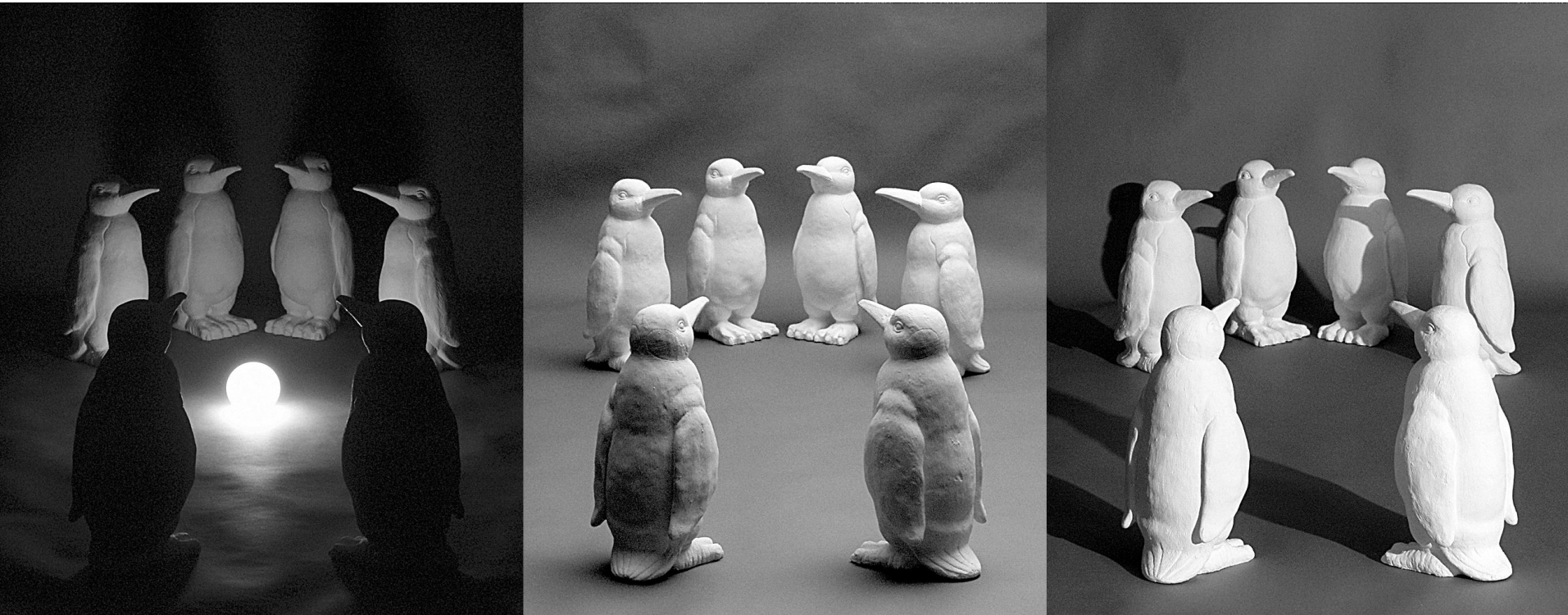


Michelangelo 1475-1564



Why is image understanding difficult?

- Variability: different lighting



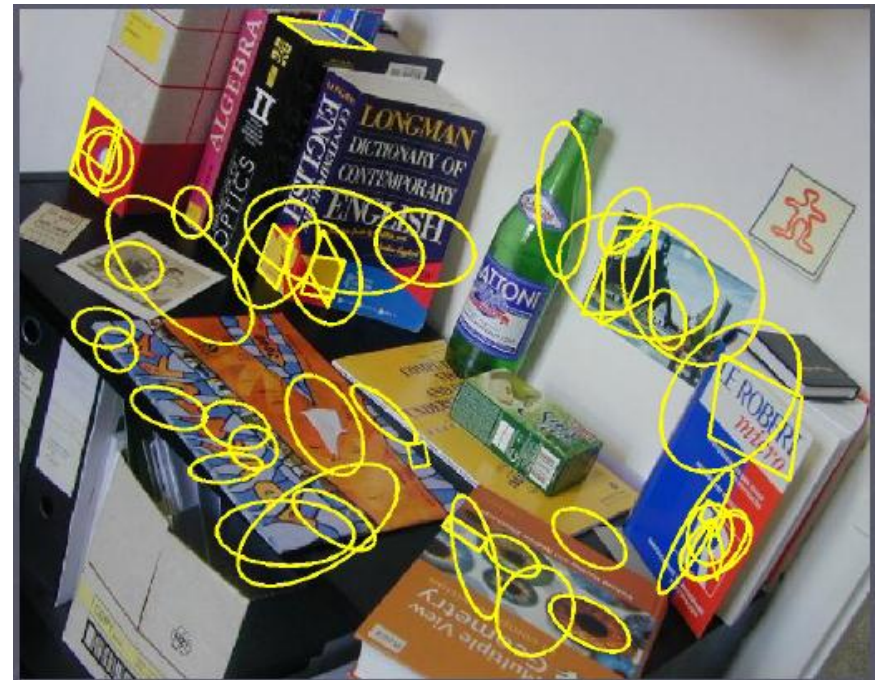
Reducing variability by using local cues

- Motivation: stitching panoramas
 - Find distinctive points
 - Find an alignment that matches these points



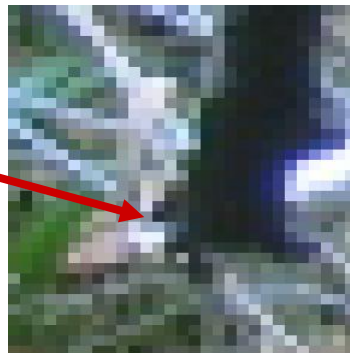
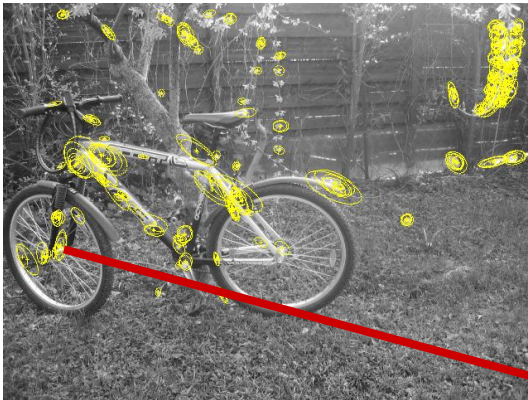
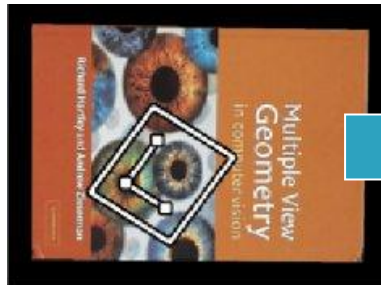
Reducing variability by using local cues

- Motivation: stereo matching



Reducing variability by using local cues

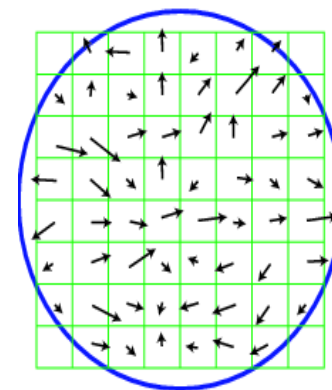
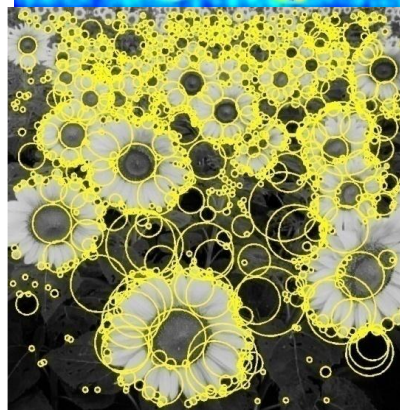
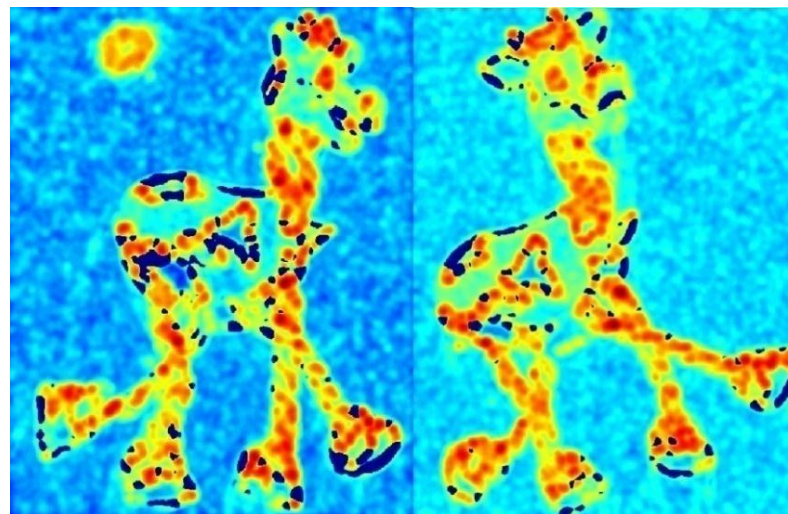
- Motivation: image retrieval object detection



Learning local models from local cues

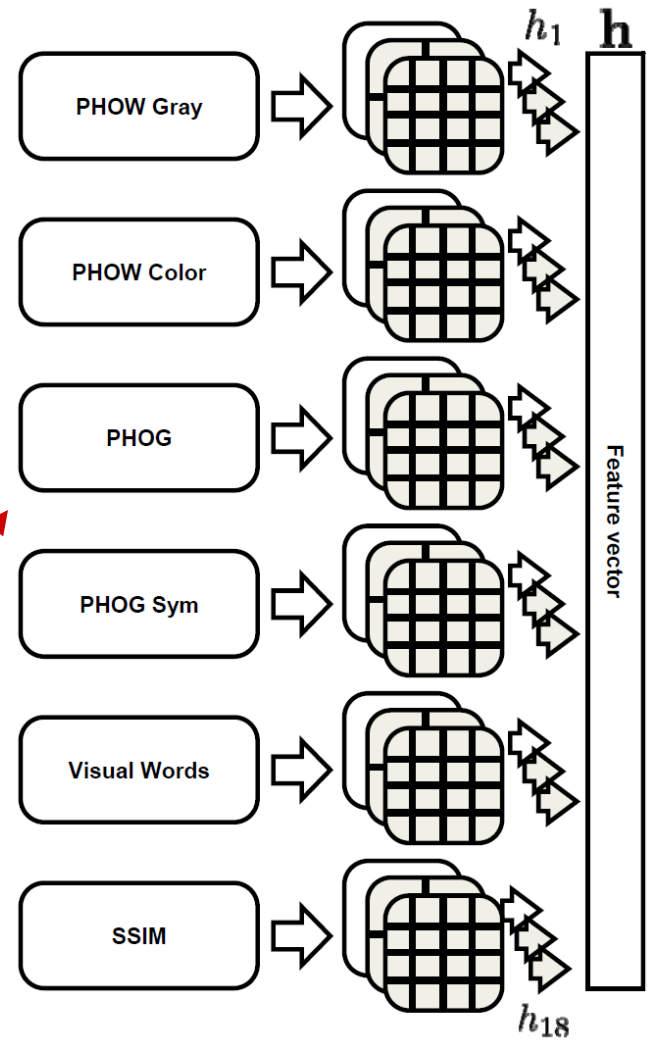
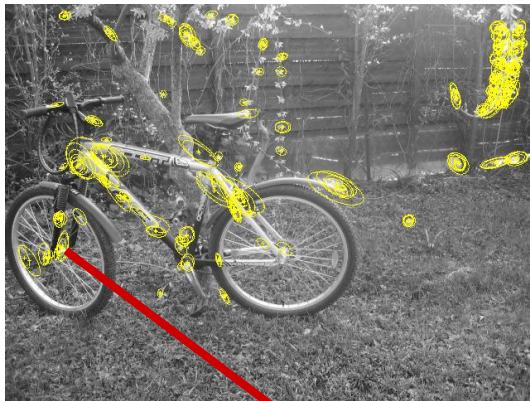
• Local features and descriptors

- Feature detectors
 - Harris-Laplace
 - LoG
 - DoG
 - Dense sampling
- Descriptors
 - SIFT
 - Shape context
 - HOG
 - Pixel comparison



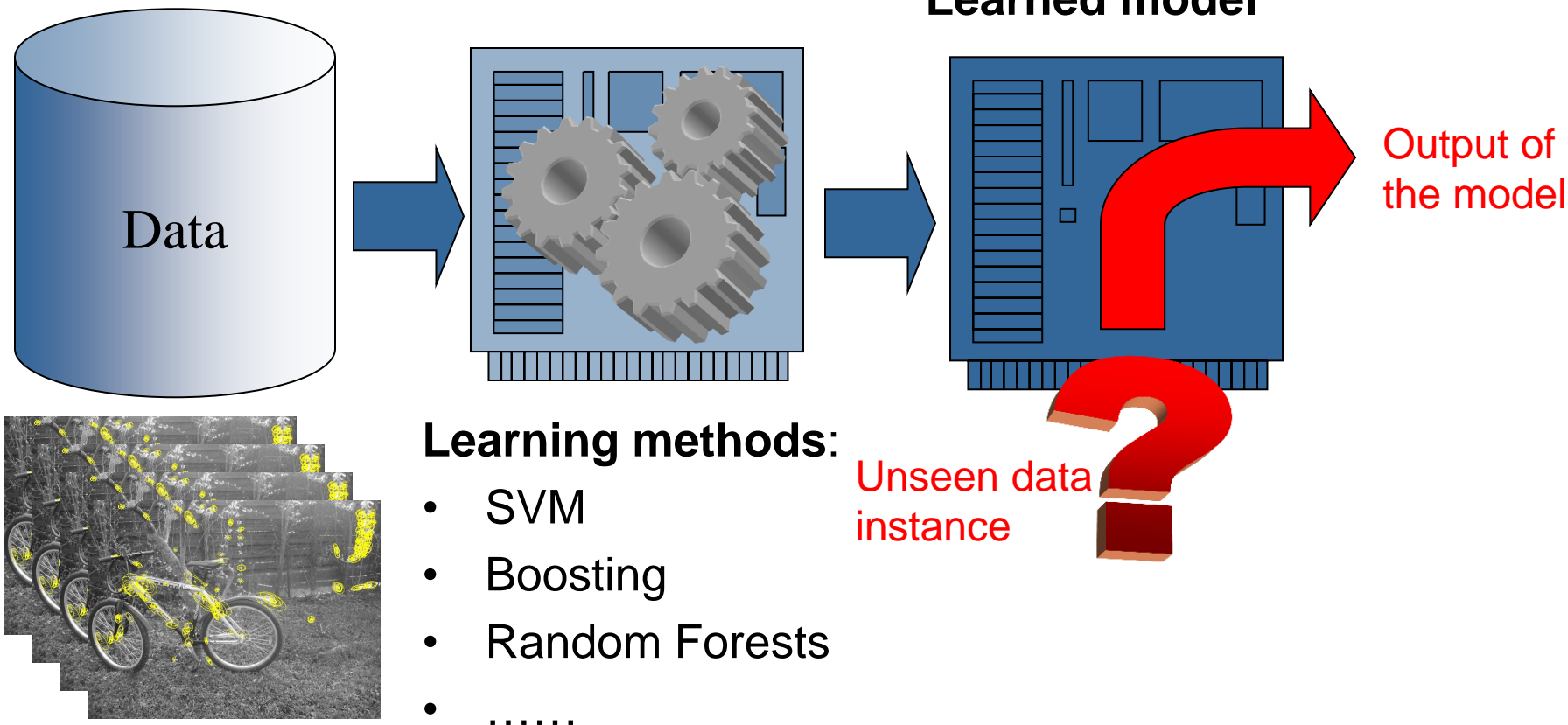
Learning local models from local cues

- Combining different descriptors



Learning local models from local cues

- Learning models from the data



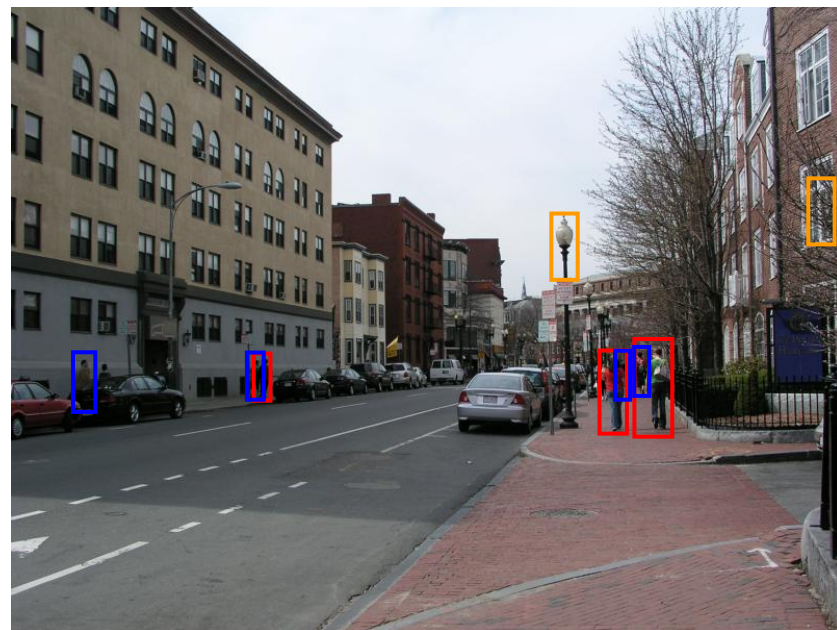
Learning local models from local cues

- Example: object detection using sliding window

- 'Local' has been the dominant paradigm in computer vision till the 2000s
- Works notoriously well for detection of rigid objects, e. g. faces

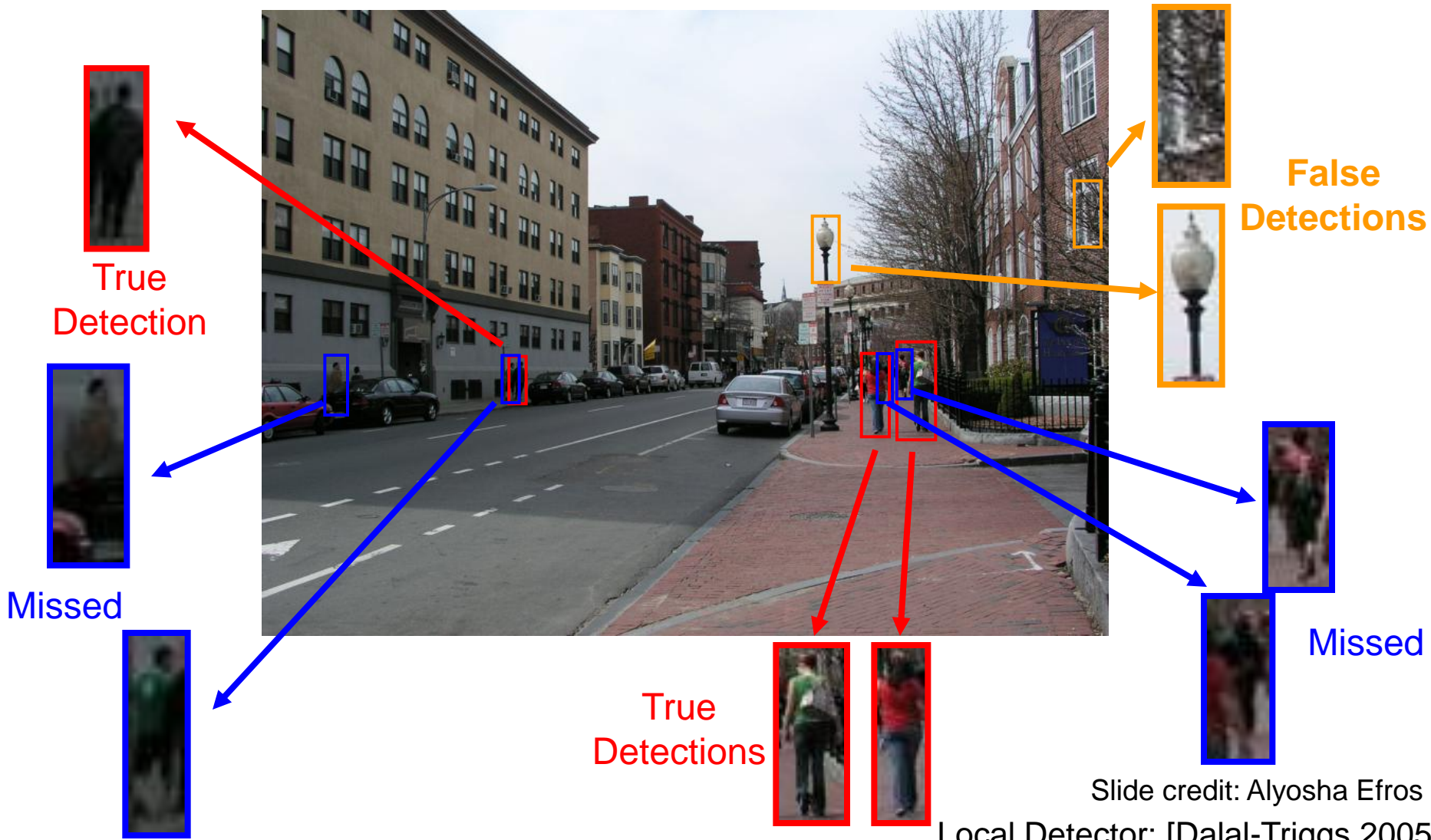
[Viola, Jones, 2001],

[Dalal, Triggs, 2005]



Learning local models from local cues

- Let's have a closer look at the results



Learning local models from local cues

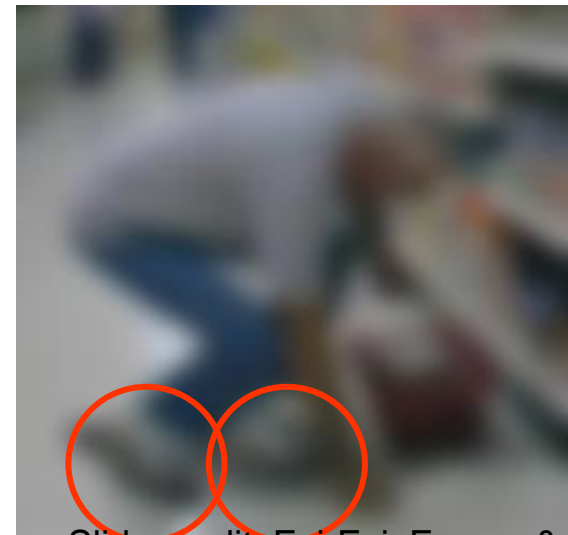
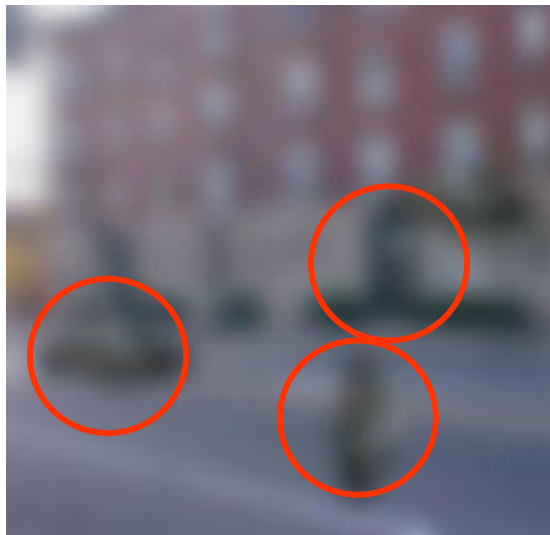
- What the detector sees



Slide credit: Alyosha Efros

Learning local models from local cues

- Local ambiguity



Slide credit: Fei-Fei, Fergus & Torralba

Learning local models from local cues

- The role of context



Slide credit: Fei-Fei, Fergus & Torralba

Learning local models from local cues

- The role of context



Slide credit: Fei-Fei, Fergus & Torralba

Constraints of the world

• The world is structured, not everything is possible

- Local cues
 - Similar appearance of similar objects
- Global constraints
 - Limited number of allowed deformations of the objects in 3d
 - Depth ordering and occlusions
 - Rules of perspective projection
 -



Chaotic world

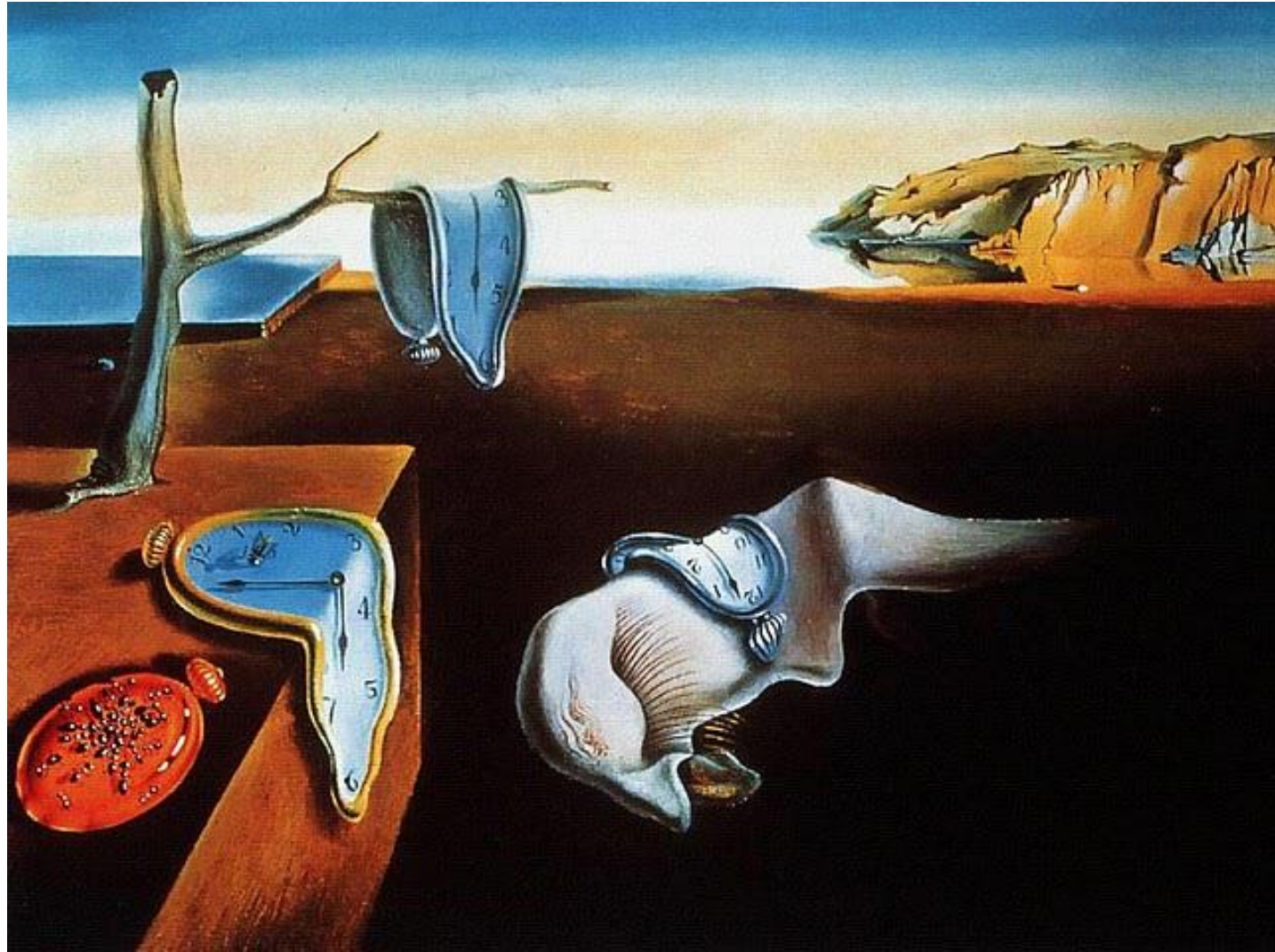


Structured world

Constraints of the world

- Limited set of allowed deformations for the objects

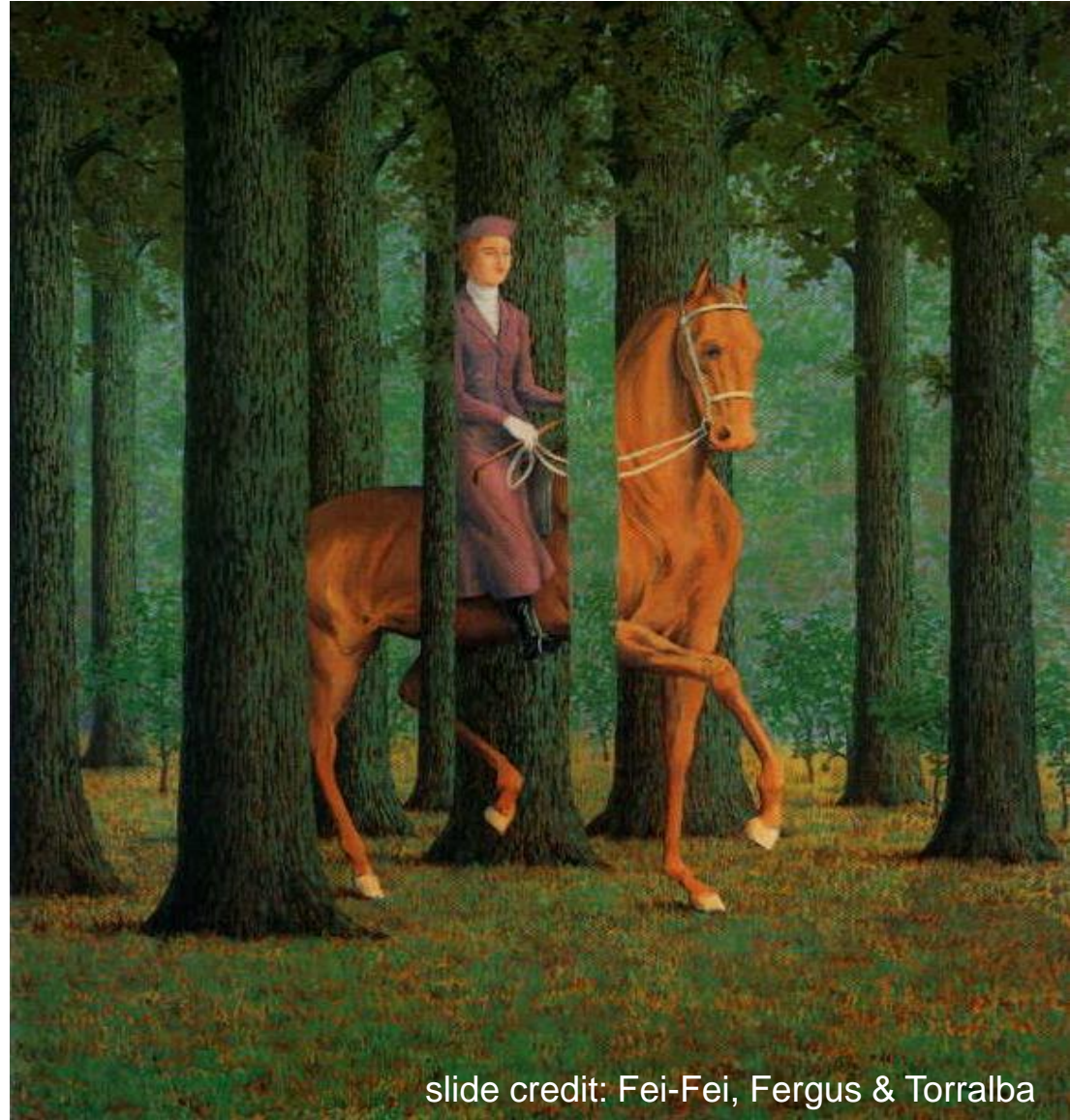
Dali, 1931



Constraints of the world

- Occlusions

Magritte, 1957



Constraints of the world

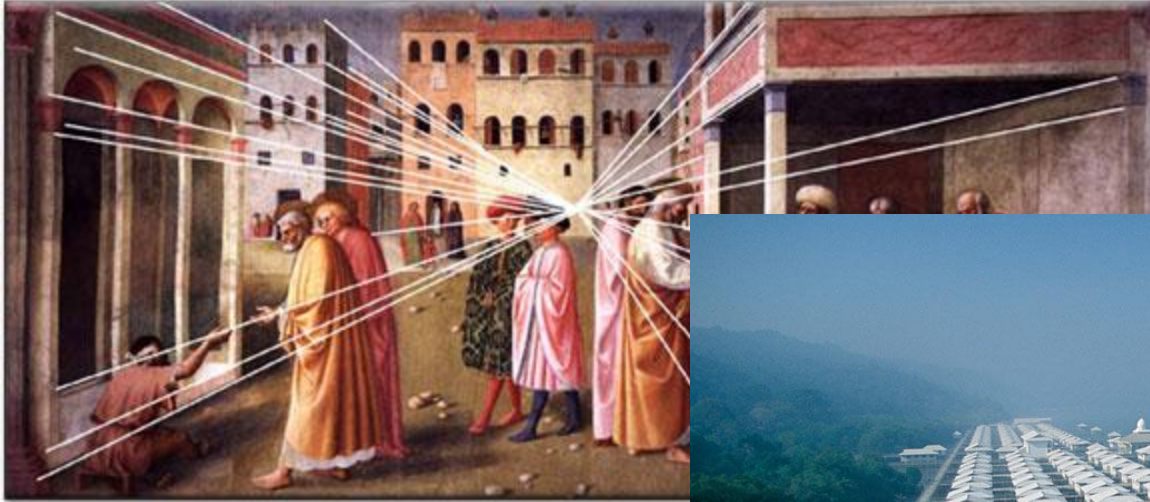
- Depth ordering



Slide credit: J. Koenderink

Constraints of the world

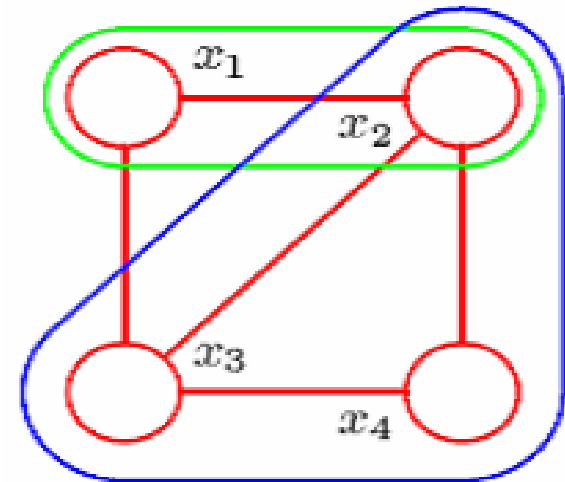
- Rules of perspective geometry



- Outline of the talk
 - The idea of graphical models
 - Examples:
 - Limiting the set of allowed deformations
 - Occlusion constraint
 - Depth ordering constraint
 - Modeling the rules of perspective geometry

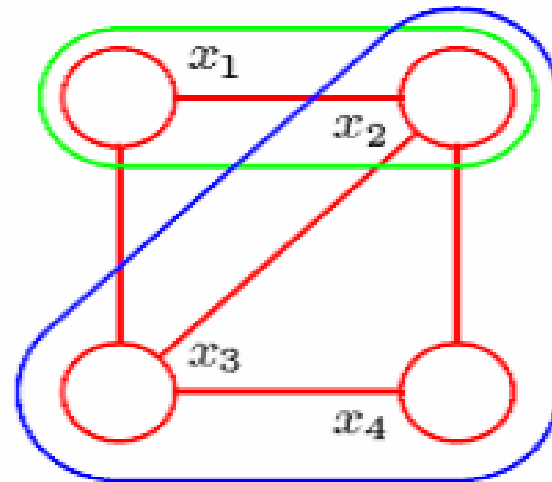


- Outline of the talk
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- Graphical models

- Graphical representation of probability distributions
- Graph-based algorithms for calculation and computation
- Capture both local cues and global constraints by modeling dependencies between random variables



Picture credit: C. Bishop

Graphical models

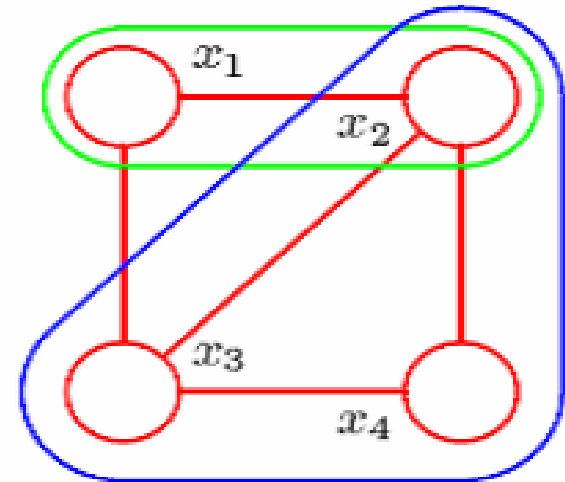
- Graph representation

- Each node corresponds to a **random variable**

- **Dependent variables** are connected with edges

- **Clique** - fully connected set of nodes in the graph

- **Maximal clique** - a clique that is not a subset of any other cliques



$$p(x_1, x_4 / x_2, x_3) = p(x_1 / x_2, x_3) p(x_4 / x_2, x_3)$$

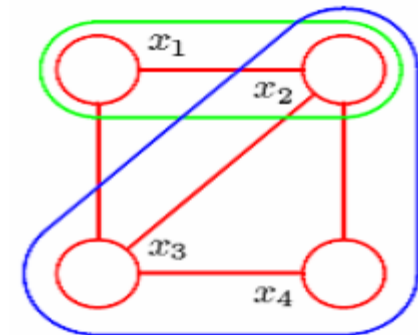
Graphical models

- Joint distribution and potentials

Joint distribution of all random variables can be written as a product of nonnegative **potentials** defined on maximal cliques:

$$p(X) = \frac{1}{Z} \prod_C \psi_C(X_C) \quad Z = \sum_X \prod_C \psi_C(X_C), \quad \psi_C(X_C) \geq 0$$

$$p(X) = \frac{1}{Z} \psi_1(x_1, x_2, x_3) \psi_2(x_2, x_3, x_4)$$

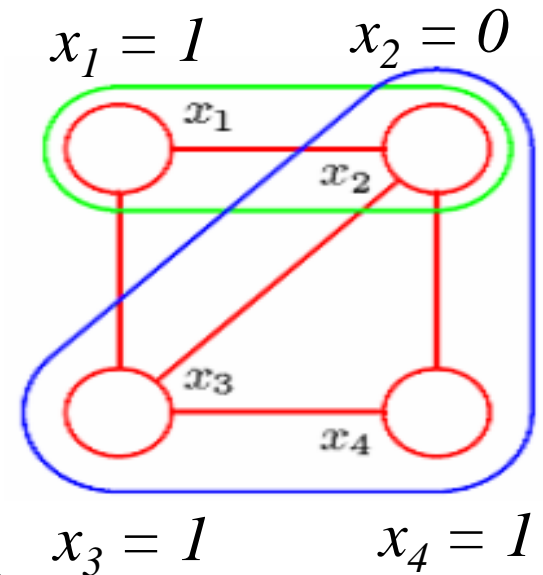


Graphical models

- MAP-inference and energy function

Maximum a-posteriori (MAP) inference - find the values of all variables in the graphical model that maximize the joint probability

$$\begin{aligned} \arg \max p(X) &= \arg \max \frac{1}{Z} \prod_c \psi_c(X_c) = \\ &= \arg \max \exp\left(-\sum_c E_c(X_c)\right) = \\ &= \arg \min \sum_c E_c(X_c) \end{aligned}$$



Energy function: $E(X) = \log P(x) = \sum_c E_c(X_c)$

MAP-inference = energy minimization

Graphical models

- Methods for MAP-inference
 - Many computationally efficient methods for inference in graphical models have been developed:
 - graph cuts
 - TRW
 - belief propagation
 - expectation propagation
 - MCMC
 -
 - All these methods have limitations and can be used to minimize energy functions of specific forms → the art is to find tradeoff between flexibility and tractability